

# Second-order Optimality Conditions for a Semilinear Elliptic Optimal Control Problem with Mixed Pointwise Constraints

B. T. Kien<sup>1</sup>, V. H. Nhu<sup>2</sup>, and N. H. Son<sup>3</sup>

**Abstract:** In this talk, we give a common critical cone, under which the second-order necessary and sufficient conditions for a semilinear elliptic control problem with mixed pointwise constraint, are valid. Some kinds of second-order sufficient optimality conditions are given and compared. Our results approach to a theory of no-gap second-order conditions. In order to obtain the results, we reduce the problem to a special mathematical programming problem in which the constraint sets are G-polyhedral and then we use some tools of variational analysis and techniques of semilinear elliptic equations to analyze second-order conditions.

---

<sup>1</sup> Institute of Mathematics, Vietnam Academy of Science and Technology, 18 Hoang Quoc Viet Road, Hanoi, Vietnam  
*btkien@math.ac.vn*

<sup>2</sup> Faculty of Information Technology, National Institute of Education Management, 31 Phan Dinh Giot, Hanoi, Vietnam  
*vhuunhu1983@gmail.com*

<sup>3</sup> School of Applied Mathematics and Informatics, Hanoi University of Science and Technology, 1 Dai Co Viet, Ha Noi, Vietnam  
*nguyenson15583@gmail.com*