

# On the Convergence Property for Differential Algebraic Equations Modeling Transient Hydraulic Circuits

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**Abstract:** Consider the differential algebraic equation

$$\Lambda_1(x) := A\dot{x} + F(x, t, \nu) = 0, \quad t \in I_t = (-\infty, +\infty), \quad (1)$$

where  $A$  is a constant  $(n \times n)$ -matrix,  $F(x, t, \nu)$  is an  $n$ -dimensional vector-function,  $x \equiv x(t)$  is a desired vector-function,  $\nu \in \mathcal{N} = (-\nu_0, \nu_0)$  is a scalar parameter. It is assumed that

$$\det A = 0.$$

Let system (1) have a solution  $\eta(t, \nu)$ ,  $t \in I_t$ , and herewith all other solutions  $x(t, \nu; t_0, x_0)$  of system (1) satisfy the following condition

$$\lim_{t \rightarrow \infty} [x(t, \nu; t_0, x_0) - \eta(t, \nu)] = 0, \quad x_0 = x(t_0, \nu).$$

Then we say that system (1) possesses the convergence property, and the solution  $\eta(t, \nu)$  possesses the contraction property.

In this talk we discuss convergence and contraction properties of differential algebraic equations of the form (1) modeling transient hydraulic circuits.

This work has been supported by the Russian Foundation for Basic Research, projects N 11-01-00639, 11-01-93005.

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