

# Post-Correction Strategies for Perturbed Nonsmooth Equations

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**Abstract:** Nonsmooth equations arise in many applications, such as contact problems or constrained optimal control problems, and variational inequalities in general. We consider nonsmooth operator equations of the form

$$u = \Pi(g(\theta) - G(\theta)u)$$

where  $G(\theta)$  is an operator with smoothing properties,  $u$  denotes the unknown and  $\Pi$  is some nonsmooth projection. The problem and hence the solution  $u[\theta]$  depend on a parameter  $\theta$  which models perturbations. We investigate several post-correction strategies to recover  $u[\theta]$  from a nearby nominal solution  $u[\theta_0]$ . With an appropriate strategy, the approximation error in the  $L^\infty$  norm can be shown to be  $o(\|\theta - \theta_0\|)$ , while for other strategies this holds only in weaker norms. Numerical examples will illustrate our results.

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