

Adaptive FEM for Nonlinear Problems

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Abstract: Rigorous mesh adaptation in the finite element approximation of nonlinear variational problems is based on a posteriori error estimates. Such estimates may be derived by employing ideas of optimal control theory especially the concept of an adjoint. This lecture presents an approach towards goal-oriented adaptivity in which the error in a functional of the solution is written in terms of primal and dual residuals (see [1] and [2]). For evaluating the resulting a posteriori error estimate an associated linear dual problem has to be solved. The linearization leaves a remainder term which is cubic in the errors and is neglected in the course of the refinement process. In this way mesh adaptation is oriented at the pre-defined goal of the computation and reaches high computational efficiency. This general approach can be used in the context of boundary value problems (see [5]), optimal control problems (see [3]) as well as eigenvalue problems (see [4]).

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